

Definition: Parametric Curve, Parametric Equations

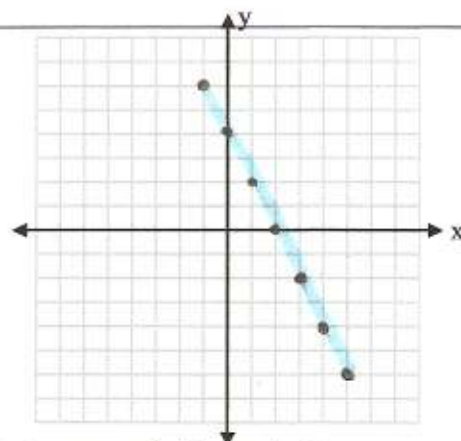
The graph of the ordered pairs x, y where $x = f(t)$ and $y = g(t)$ are functions defined on an interval I of t -values is a **parametric curve**. The equations are **parametric equations** for the curve, the variable t is a **parameter**, and I is the **parameter interval**.

Example 1: BY HAND.

$x(t) = 2 - t$ AND $y(t) = 2t$

Fill in the table of values.

t	-3	-2	-1	0	1	2	3
x	5	4	3	2	1	0	-1
y	-6	-4	-2	0	2	4	6



Using the chart above, the domain for " t " consists of the integers -3 through 3.

Therefore, our graph consists of points.

If we change the domain of " t " to $[-3, 3]$ (the real numbers between -3 and 3), the graph becomes a line segment with endpoints (5, -6) and (-1, 6).

The domain of the curve is $[-1, 5]$. The range of the curve is $[-6, 6]$.

If you eliminate " t ", what would the equation become?

$x = 2 - t$

$x - 2 = -t$

$-x + 2 = t$

$y = 2t$

$y = 2(-x + 2)$

$y = -2x + 4$

Is this a function? yes Why or why not? passes VLT

Example 2: BY CALCULATOR (same equations).

- Go to "MODE" and change to parametric mode - "PAR"
- Go to "y=" and put in $x(t)$ and $y(t)$.
- Got to WINDOW and looking at your chart above, let's set our window.

T min = -3

T max = 3

T step = .1

X min = -2

X max = 6

X step = 1

Y min = -7

Y max = 7

Y step = 1

← changes how quickly calc. graphs

making sure to see the endpoints

- Now graph and check your graph against the calculator graph.
- Check your table above against the calculator table.

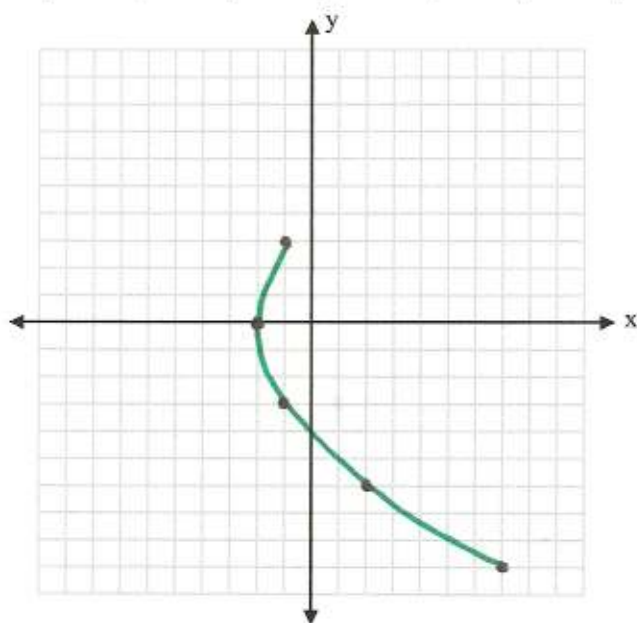
Graphing Parametric Equations BY HAND and USING THE CALCULATOR

Example 3: For the given parameter interval, graph the parametric equations.

$$x = t^2 - 2 \text{ AND } y = 3t$$

a. $-3 \leq t \leq 1$

t	-3	-2	-1	0	1
x	7	2	-1	-2	-1
y	-9	-6	-3	0	+3



Endpoints:

$(7, -9)$ and $(-1, 3)$

Domain:

$[-2, 7]$

Range:

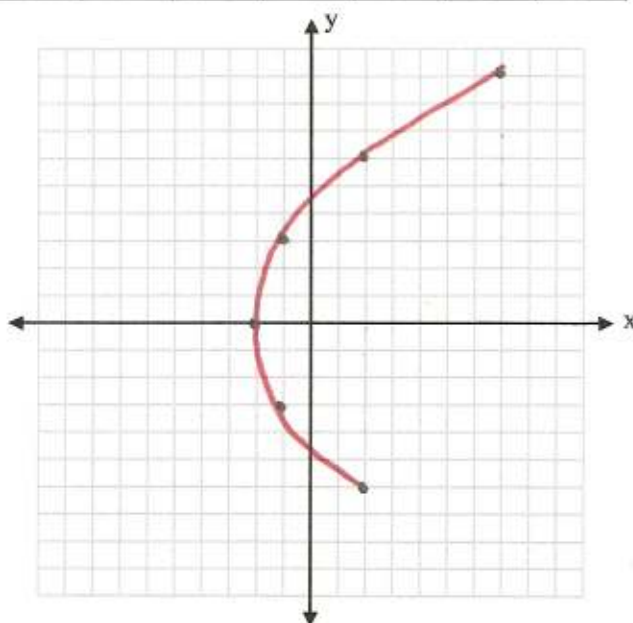
$[-9, 3]$

Function? Why or why not?

no; fails VLT

b. $-2 \leq t \leq 3$

t	-2	-1	0	1	2	3
x	2	-1	-2	1	2	7
y	-6	-3	0	3	6	9



Endpoints:

$(2, -6)$ and $(7, 9)$

Domain:

$[-2, 7]$

Range:

$[-6, 9]$

Function? Why or why not?

no; fails VLT

For the parametric equations in the above example, eliminate the parameter. What would the equation become?

$$y = \frac{3t}{3}$$

$$t = \frac{y}{3}$$

$$x = t^2 - 2$$

$$x = \left(\frac{y}{3}\right)^2 - 2$$

$$x = \frac{y^2}{9} - 2$$