

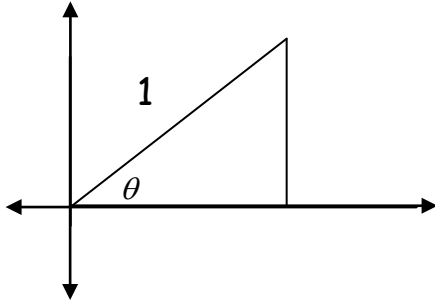
Pre-Calculus NOTES

Sections 4.2 and 4.3

Name: _____

You should have the handout titled "MEMORIZE OR PERISH" in front of you during these notes.

Now, we will start by explaining the Pythagorean identities. Please realize that $\sin^2 \theta = (\sin \theta)^2$.

	Where does $\sin^2 \theta + \cos^2 \theta = 1$ come from?
	Where does $\tan^2 \theta + 1 = \sec^2 \theta$ come from?
	Where does $\cot^2 \theta + 1 = \csc^2 \theta$ come from?

Example 1: Verify the following Pythagorean identities for the given value of θ .

a. $\sin^2 \theta + \cos^2 \theta = 1$ for $\theta = 30^\circ$	b. $\tan^2 \theta + 1 = \sec^2 \theta$ for $\theta = 45^\circ$	c. $\cot^2 \theta + 1 = \csc^2 \theta$ for $\theta = 60^\circ$

REMINDER: What does it mean to be a reciprocal?

The product of a number and its reciprocal will always equal _____.

Example 2: Use definitions (x , y , and r) to prove each of the following. SHOW ALL STEPS.

a. Prove that $\csc \theta = \frac{1}{\sin \theta}$.

b. Prove that $\tan \theta = \frac{\sin \theta}{\cos \theta}$.

c. Prove that $\tan^2 \theta + 1 = \sec^2 \theta$.

d. Prove that $\sin^2 \theta = 1 - \cos^2 \theta$.